## REPORT DOCUMENTATION PAGE

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A very substantial number of results were obtained during this contract in the area of multivariate model building and model identification. A list of publications in which the Air Force Contract is mentioned appears below. We are continuing this work in the follow on contract, AFOSR 90-0103. The research monograph "Spline Models for Observational Data" by the PI was published by The Society for Industrial and Applied Mathematics in March 1990 as volume 59 in the prestigious CBMS-NSF Regional Conference Series in Applied Mathematics. Although the actual writing of this monograph was not supported by the AFOSR, a number of research results obtained under AFOSR sponsorship are discussed in it. We have acknowledged in the Foreword the research support of the AFOSR.

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## MULTIVARIATE MODEL BUILDING AND MODEL IDENTIFICATION AFOSR-87-0171

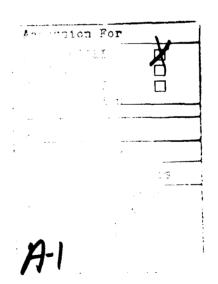
Grace Wahba, PI

Final Report

Date Submitted: April 8, 1990

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